

Solid body: No contribution of c.m. and Rotation but **Vibration**

3 directions

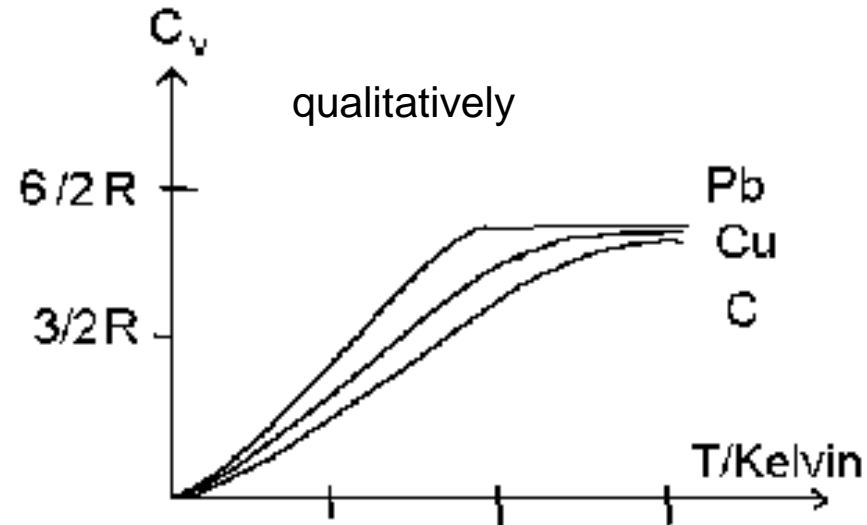
->3 degrees of freedom **kinetic**

->3 degrees of freedom **potential**

6 degrees of freedom with $c_{Mol}=3R$

Law of
Dulong-Petit

But here again,
dependence on temperature



Microscopically:

Up until now we used an atomistic view! Now view the phenomena

Quantity of heat:

$$\Delta Q = C \cdot M \cdot \Delta T$$

M: Mass of solid body

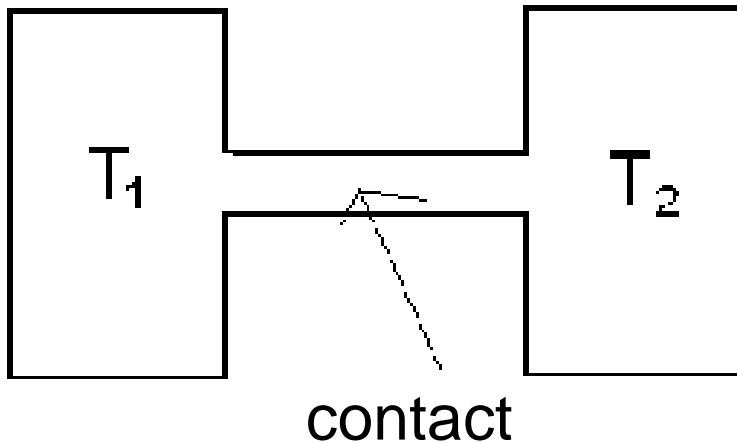
C: Capacity of heat,

$$[Q] = J, [C] = \frac{J}{kg \cdot K}$$

Temperature increase: $C=4186 \text{ J/K}$ per liter water under following conditions:

$$\Delta T = 1K \quad \text{at} \quad T = 15^{\circ} \text{Celsius} \Rightarrow Q = 4186J$$

Further conclusions from chapter. 5.1-5.3.



a) Are two bodies in contact

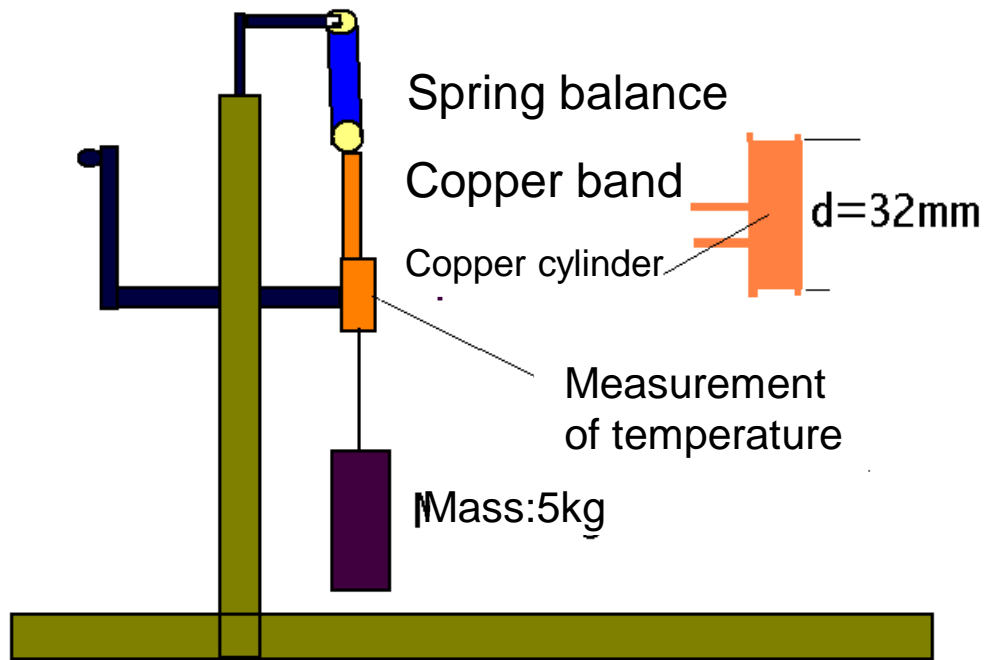
$$\Rightarrow T_1 \leftrightarrow T_2$$

settle on T !

b) $T(T_1, T_2, M_1, M_2, C_1, C_2)$

c) Independent of kind of contact

Measurement: Mechanical equivalent of heat



10 turns

$\approx 1\text{m}$

Mass copper-cylinder=119.67g

Mass copper band=5.85g

$\Sigma=125.52\text{g}$

Thermic capacity

Cu: $C_{\text{Cu}}=0.092\text{cal/gK}$

$$1. E_{\text{pot}}=mgh=5 \cdot 9.81 \cdot 1\text{kg} \cdot \text{m}^2 \cdot \text{s}^{-2}$$
$$\approx 50\text{N} \cdot \text{m}=50\text{J}=\mathbf{50\text{Ws}}$$

$$2. M_{\text{Cu}} \cdot C_{\text{Cu}} \cdot \Delta t=125.52 \cdot 0.092 \cdot 1 \cdot \text{g} \cdot \text{cal} \cdot \text{K} / \text{g} \cdot \text{K}$$
$$=11.5\text{cal}$$

$$11.5 \cdot 4.184 = \mathbf{48.116}$$

Calories \Rightarrow Joule
or Ws

Temperature

Defined by fixed points

Temperature, in case of water changes its state of matter!

Melt	solid -> liquid	0 ⁰ Celsius
Boil	liquid -> gaseous	100 ⁰ Celsius

Celsius-Scale
C

Melt	solid -> liquid	32 ⁰ Fahrenheit
Boil	liquid -> gaseous	212 ⁰ Fahrenheit

Fahrenheit-Scale
1714
F

At normal air pressure

Absolute thermodynamic scale of temperature

Point of zero: -273.15⁰ Celsius

Unit: 1 Kelvin = 1K



Movement of molecules beeing at rest

$$\text{e.g.: } T(\text{C}) = T(\text{K}) - T_0(\text{K}); T_0 = 273.15$$

Change of volume: Cube with length of the edge l_0

$$V(T) = [l(T)]^3 = l_0^3(1 + \alpha \cdot \Delta T)^3 \approx l_0^3(1 + 3 \cdot \alpha \cdot \Delta T)$$

$$l_0^3 = V_0; 3 \cdot \alpha = \gamma \quad \text{cubic coefficient of expansion}$$

Water at 18 ⁰ C	$\gamma = 0.18 \cdot 10^{-3}/K$
Ethanol	$\gamma = 1.1 \cdot 10^{-3}/K$
Mercury	$\gamma = 0.18 \cdot 10^{-3}/K$

Dependence of density on temperature

$$\rho = \frac{M \text{ (independent of } T)}{V} \approx \frac{M}{V_0(1+\gamma \cdot \Delta T)} = \frac{\rho_0}{1+\gamma \cdot \Delta T} \approx \rho_0 \cdot (1 - \gamma \cdot \Delta T)$$

There are Anomalies e.g.: H₂O : Largest density at 4⁰

5.5. State variables of ideal gases

Volume V , Pressure P ,
Temperature T
In each case one quantity
stays constant!

a) $T = \text{constant}$.
"isotherme" change of state

$PV = \text{constant}$ Law: Boyle-Mariotte

b) $P = \text{constant}$ "isobare" change of state

$$V = V_0 \cdot [1 + \gamma \cdot t] \quad t = T - T_0 \quad \text{Law: Gay-Lussac}$$

$$V = V_0 \cdot \left[1 + \frac{1}{T_0} (T - T_0) \right] = V_0 \frac{T}{T_0} \Rightarrow \quad \gamma \text{ equal for all gases with}$$
$$\gamma = \frac{1}{273.2} = \frac{1}{T_0}$$
$$V = \frac{V_0}{T_0} \cdot T \Rightarrow \frac{V}{T} = \text{constant}$$

c) $V = \text{constant}$
"isochore" change of state

$$P = P_0 \cdot (1 + \beta \cdot t)$$

P_0 : Pressure at 0°C

β : coefficient of pressure,

Measurement of Temperature

Physical phenomena are T-dependent → **Thermometer**

Liquid thermometer: **Change of volume**

$$\Delta V = \Delta V(T)$$

Bimetal thermometer: Different extensions of metal band

Heat: $\Delta Q = C \cdot M \cdot \Delta T$

Temperature T a measure for energy within the body,

called heat !

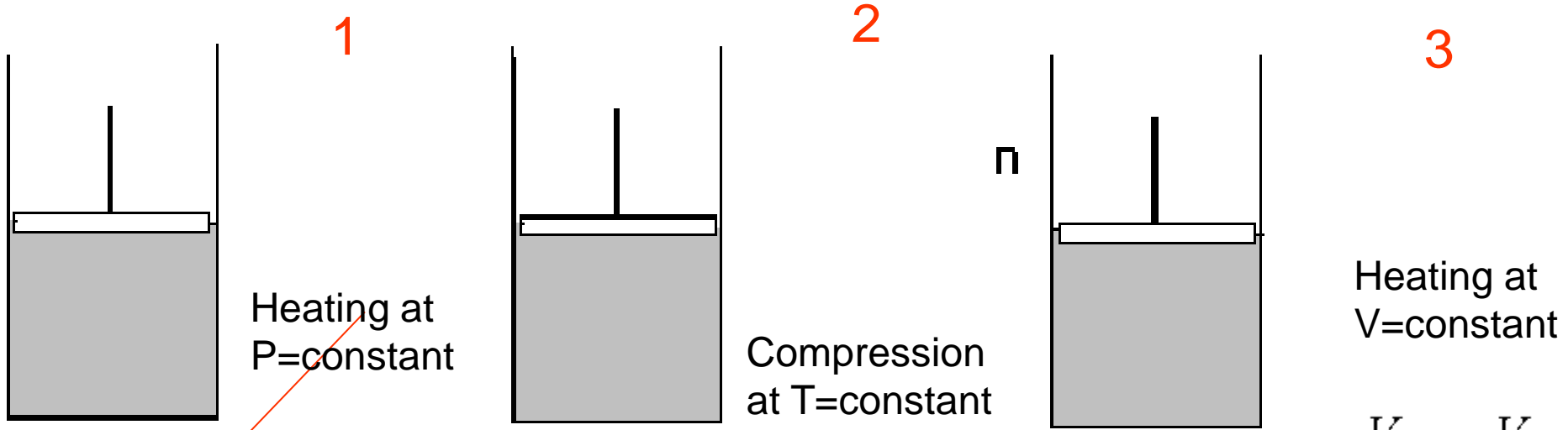
5.4. Extension due to heat of solid and liquid bodies

Bar: Linear coefficient of extension α

$$l(T) = l(T_0) + \Delta l(T - T_0) = l_0 + \alpha \cdot l_0 \cdot \Delta T = l_0 \cdot (1 + \alpha \cdot \Delta T)$$

Examples: **Al**: $\alpha = 23.8 \cdot 10^{-6}/K$, **Quartzglass**: $\alpha = 0.5 \cdot 10^{-6}/K$

Conection between β and γ



$P_0 \quad V_0 \quad T_0$

T_1
 $P_1 = P_0$

$T_2 = T_1$

$V_2 = V_0$

$$V_1 = V_0(1 + \gamma t)$$

$$P_2 \cdot V_2 = P_1 \cdot V_1 =$$

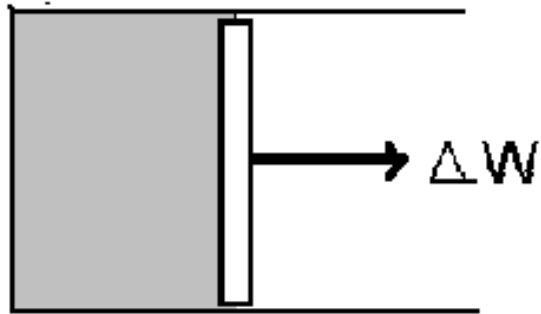
$$P_0 \cdot V_0(1 + \gamma t)$$

$$P_2 = P_0(1 + \beta t) \Rightarrow V_2 P_2 = V_0 P_0(1 + \beta t) \Rightarrow$$

$$\beta = \gamma$$

5.6. 1. Main law of thermodynamics

Conservation of energy



Total energy of a closed system remains always constant

$$\Delta Q = \Delta U + \Delta W$$

added thermal energy = inner energy + work done

$$\Delta U \sim \Delta T$$

$$\Delta W = F \cdot ds = \frac{F}{A} \cdot A \cdot ds = P \cdot dV$$

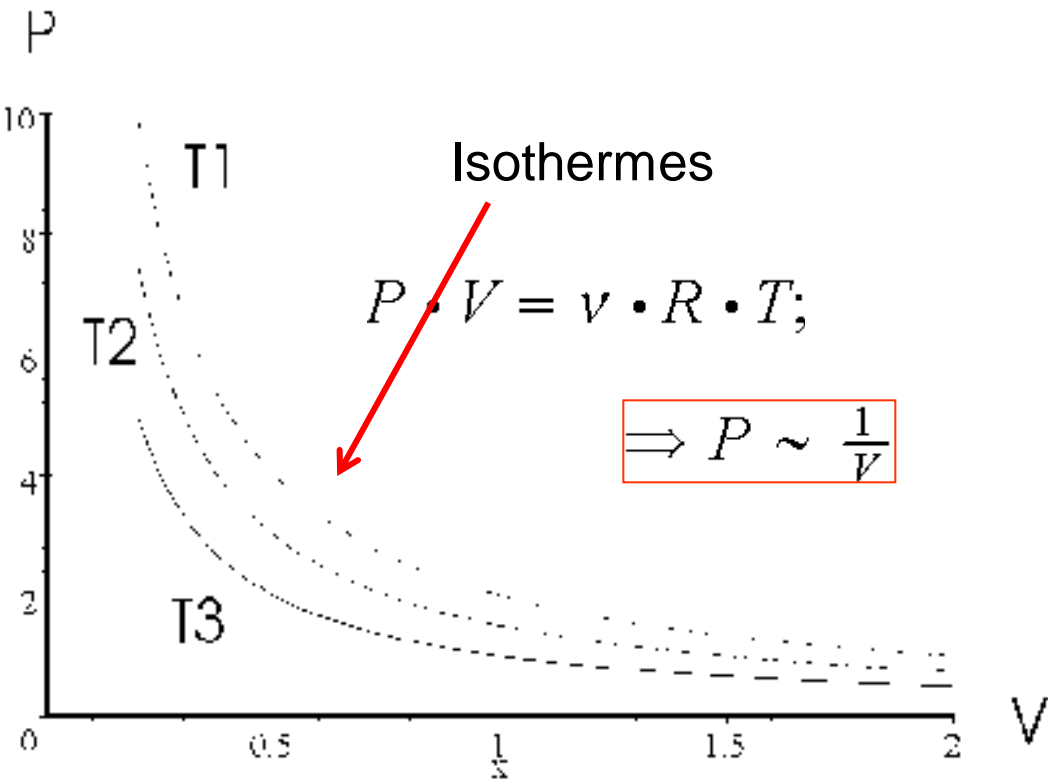
$$dQ = dU + dW$$

$$dQ = c_V dT + PdV$$

It is important to realize that in physics today we have no knowledge of what energy is...it is an abstract thing.

R. Feynman

Isothermic changes of states

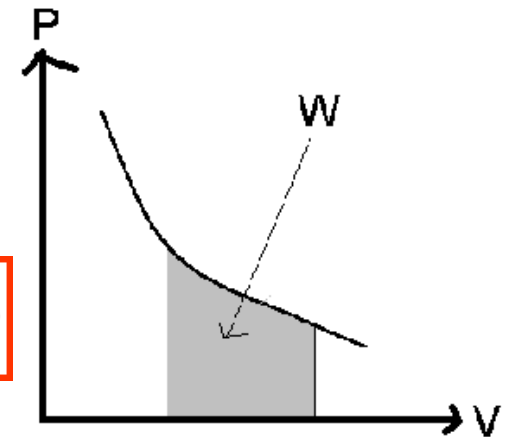
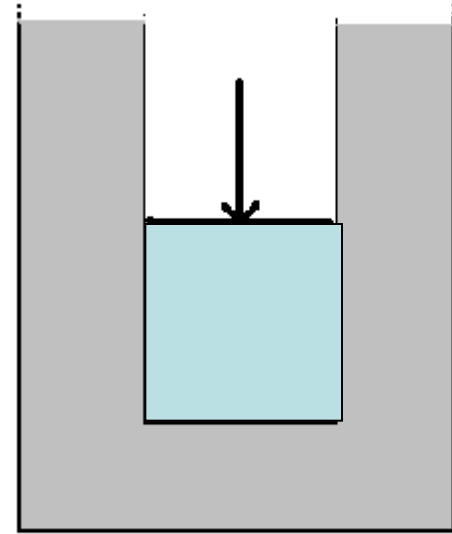


from first law: $dQ=dW=PdV$ or

$$W = \int_{V_1}^{V_2} P dV = \nu \cdot R \cdot T \int_{V_1}^{V_2} \frac{dV}{V} = \nu \cdot R \cdot T \cdot \ln \frac{V_2}{V_1}$$

Experiment:

Bath of heat: $T=\text{constant}$



Adiabatic changes of states

No exchange of heat within surroundings $\rightarrow dQ=0$

1. Law $\rightarrow dU + PdV = 0$ with $dU = \nu \cdot C_V \cdot dT \Rightarrow$

and from $P \cdot V = \nu \cdot R \cdot T$

$$P \cdot dV + V \cdot dP = \nu \cdot R \cdot dT \rightarrow dT = \frac{1}{\nu \cdot R} \{P \cdot dV + V \cdot dP\}$$

with main law: $\frac{C_V}{R} \{P \cdot dV + V \cdot dP\} + P \cdot dV = 0$

$$P \cdot dV(C_V + R) + C_V V \cdot dP = 0 \quad P \cdot dV \frac{C_V + R}{C_V} + V \cdot dP = 0$$

$$\gamma \cdot P \cdot dV = -V \cdot dP \quad \left(\gamma \frac{dV}{V}\right) + \left(\frac{dP}{P}\right) = 0$$

Integration:

$$\gamma \ln V + \ln P = \ln C \Rightarrow$$

or because $PV \sim T$

$$P \cdot V^\gamma = C$$

$$T \cdot V^{\gamma-1} = \text{constant}$$

or because $V \sim T/P$

C constant of integration

$$T^\gamma \cdot P^{1-\gamma} = \text{constant}$$

Example: Pneumatic lighter

$$V_1 \rightarrow \frac{V_1}{10} \rightarrow \dots \quad \text{with}$$

$$T_1 \cdot V_1^{\gamma-1} = T_2 \cdot V_2^{\gamma-1} \Rightarrow T_2 = T_1 \left(\frac{V_1}{V_2} \right)^{\gamma-1}$$

$$\gamma = 1.4$$

for air

$$\text{or } 293\text{K} \cdot 10^{0.4} = 293 \cdot 2.51 = 735.43\text{K} = 463^\circ\text{C}$$

Comparison Adiabates \leftrightarrow Isothermes

