

Latent heat quantities:

Requires transition of a certain quantity of matter starting from phase i towards phase k with heat quantity Q_{ik}

reverse from phase k into phase i

a heat quantity Q_{ki} ,

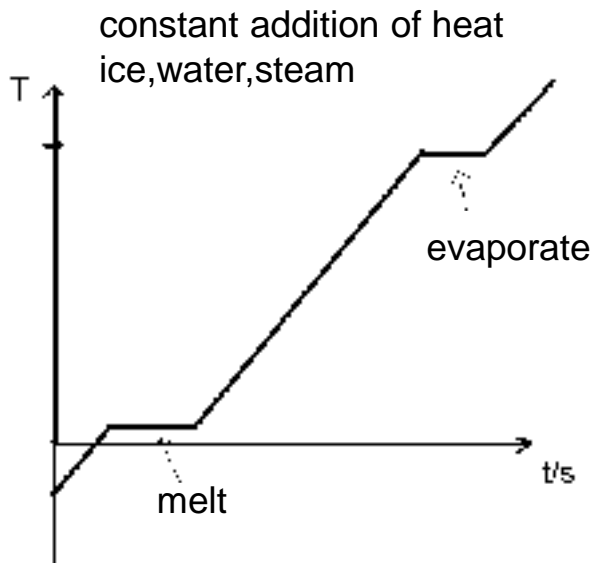
to obtain $Q_{ki} = -Q_{ik}$

At $k \rightarrow i$ gets (latent) heat free again!

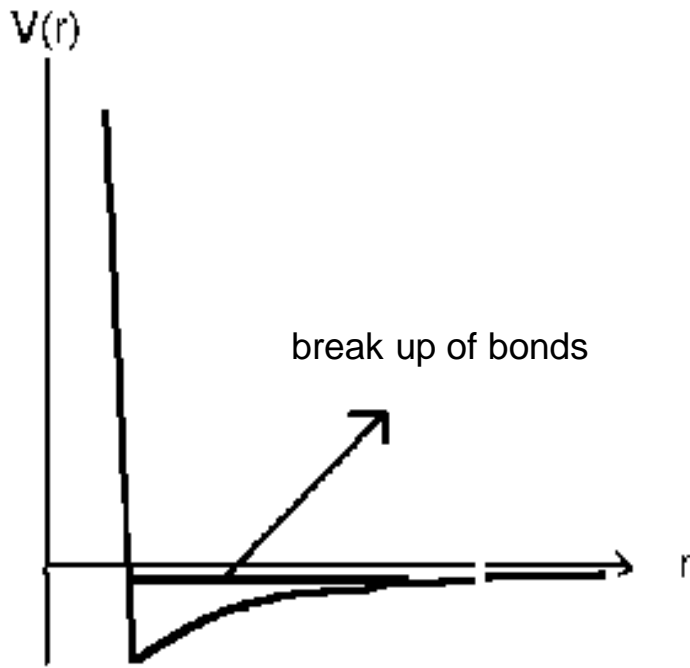
$\lambda_{ik} = \frac{Q_{ik}}{m}$: specific melt- ($\lambda_{solid,liquid}$) ,-vapor- ($\lambda_{liquid,steam}$)

and heat of sublimation ($\lambda_{solid,steam}$)

$$(\lambda_{solid,steam}) : [\lambda_{ik}] = \frac{J}{kg}$$



Because within a time region $\Delta T=0 \rightarrow$
the added heat quantity
increases potential energy



Vapor pressures (saturated vapor): p_s water
 $(0^\circ) : 610Pa,$

P_s water(20°) : $2337Pa$

heat of evaporation comes out of surroundings

Exp.:

Äthyläther ($5.87 \cdot 10^4 Pa, T = 20^\circ$)

Example: Water:

$$\lambda_{solid,liquid} = 3.3 \cdot 10^5, \lambda_{liquid,steam} = 2.3 \cdot 10^6$$

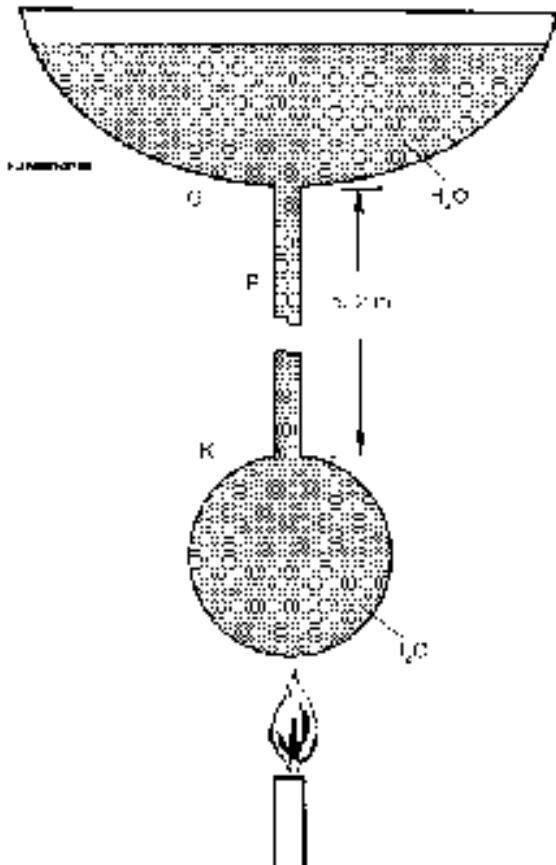
Equilibrium of phases at interfaces e.g:
 liquid - steam , all the same molecules come in and out.

Boil/Condensation

given $p_s >$ outer pressure \rightarrow steam-bubbles inside

if vapor pressure of liquid = outer pressure \rightarrow boil!

e.g: Geyser (changing pressure on piston)



changes of phases need seeds of condensation / cristallisations

Therefore, one observes by missing of those:

delay of condensation and boil

If $p_s <$ Outer vapor pressure :
Condensation
e.g.:
Air humidity

$$\varphi_{rel} = \frac{\varphi_a}{\varphi_S} = \frac{P_W}{P_S} \quad \text{with } \varphi_a \text{ absolute humidity (g/m}^3\text{)}$$

$\varphi_S =$ Saturated humidity (g/m³)

One has an air humidity of 40% , if the partial pressure reaches

$$P_W = 0.4 \cdot P_S(H_2O)$$

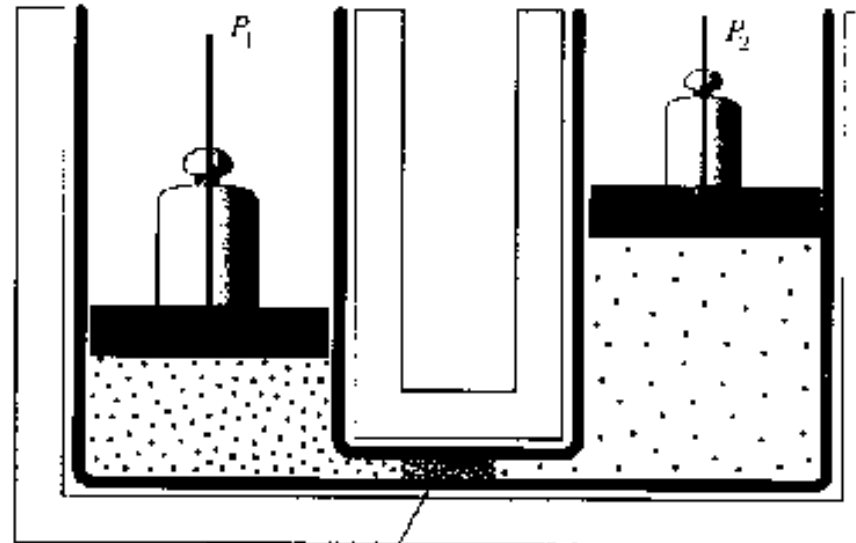
$\varphi_{rel} = 1$: Dew point ! !

Joule-Thomson-Effect and liquifaction of gases

Considered are adiabatic,
throttelt decompression
of gases:

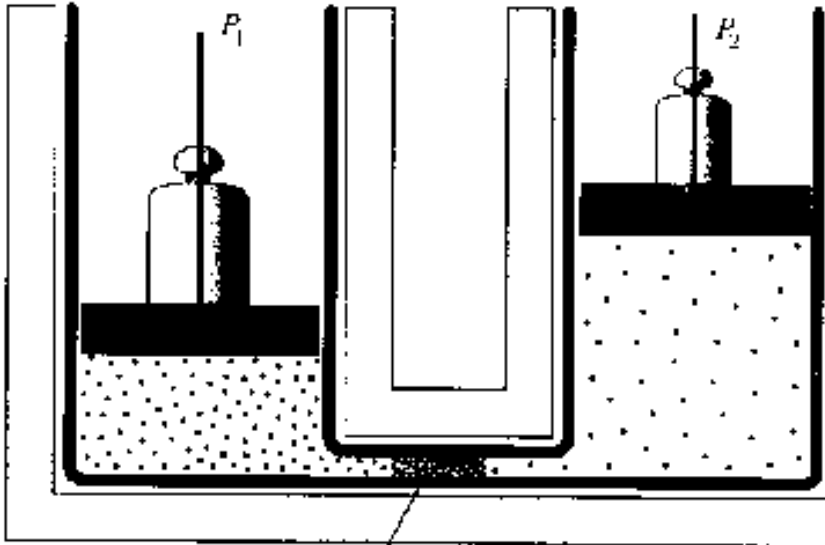
gas cell

$P_1 > P_2$



Drop in pressure via e.g. cotton wool

$$P_1 > P_2$$



Drop in pressure via e.g. cotton wool

Adiabatic expansion via Throttling valve (here wool)

Beginning: Gas $V_1, V_2 = 0$

vessel walls athermanous

$$\Delta Q = 0$$

Final: Gas completely in V_2

1. Fundamental law

$$\Delta U = -P_2 \cdot V_2 + P_1 \cdot V_1$$

Or (ideal gas):

or

On the left of the picture added displacement work

$$U_2 - U_1 = -P_2 \cdot V_2 + P_1 \cdot V_1 \Leftrightarrow$$

$$U_1 + P_1 \cdot V_1 = U_2 + P_2 \cdot V_2 = H; \text{Enthalpy}$$

$$P_1 \cdot V_1 = P_2 \cdot V_2,$$

Ideal gas: $U = c_V \cdot T, P \cdot V = R \cdot T \Rightarrow$

$$\rightarrow U_1 = U_2 \Leftrightarrow T_1 = T_2$$

$$H = (c_V + R) \cdot T = c_P \cdot T \Rightarrow dT = 0$$

Changes with real gas?

1. Internal pressure

$$\frac{a}{V^2} \quad :$$

After throttling work against van der Waals - forces

$$\Rightarrow U_1 > U_2 \Rightarrow T_2 < T_1$$

2. Covolume b:

$$P = \frac{v \cdot R \cdot T}{V-b} \quad \text{larger compared to ideal gas:}$$

Equal number of particles N
pressure of real gases

$$\Rightarrow P_1 \cdot V_1 > P_2 \cdot V_2 \Rightarrow U_1 < U_2$$

$$\text{or} \quad T_2 > T_1$$

Calculation : Van der Waals-equation

$$P = \frac{RT}{V-b} - \frac{a}{V^2}; \quad U \text{ can be written as}$$

$$U = "E_{kin}" + E_{pot} = \frac{f \text{ (degrees of freedom)}}{2} RT + \int_{\infty}^{V_1} \frac{a}{V^2} dV = -a/V_1$$

$$\Rightarrow H = U + P \cdot V = \frac{f \cdot RT}{2} - \frac{a}{V} + \left(\frac{RT}{V-b} - \frac{a}{V^2} \right) \cdot V$$

$$= RT \left(\frac{f}{2} + \frac{V}{V-b} \right) - \frac{2a}{V}$$

$$dH = \frac{\partial H}{\partial V} \cdot dV + \frac{\partial H}{\partial T} \cdot dT = 0$$

$$\Rightarrow dT = - \frac{\frac{\partial H}{\partial V} \cdot dV}{\frac{\partial H}{\partial T}} = \frac{\frac{bT}{(V-b)^2} - \frac{2a}{R \cdot V^2}}{\frac{f}{2} + \frac{V}{V-b}} dV$$

with approx. $V \approx V-b \Rightarrow dT \approx \frac{b \cdot R \cdot T - 2a}{\left(\frac{f}{2} + 1\right) R \cdot V^2} dV \Rightarrow$

Inversion temperature:

$$T_I = \frac{2a}{bR} \quad \text{e.g. for}$$

$$T < T_I : \quad \text{cooling}$$

$$T > T_I : \quad \text{heating}$$

Examples:

Temperature of inversion

CO ₂	N ₂	O ₂	He	H ₂
2050K	850K	1040K	35K	35K

Observations: air out of a tire with quick release >
Valve cools, would the tire be filled with helium,
the valve would grow warm !